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## Estimating Hull Resistance of a Pontoon by using CFD

Ngo Van He\*, Hoang Cong Liem, Ngo Van Hien

*Hanoi University of Science and Technology, Hanoi, Vietnam*

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### ABSTRACT

This paper presents our estimated results of hull resistance acting on a full-scale pontoon by a commercial Computational Fluid Dynamic (CFD). The results have been compared with those obtained by using various well-established valuable empirical formulae introduced by the International Towing Tank Conference (ITTC). The differences between the empirical formulae and the CFD results have been found and discussed.

**Keywords:** Hull, resistance, CFD, pontoon, empirical formulae.

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\*Corresponding author at: Hanoi University of Science and Technology, 1 Dai Co Viet Road, Hai Ba Trung, Hanoi, Vietnam. *E-mail addresses:* [he.ngovan@hust.edu.vn](mailto:he.ngovan@hust.edu.vn)

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**INTRODUCTION**

The hull resistance acting on the ship is essential in the ship design process. Prediction of hull resistance working on hull of a vessel is critical at the first step in ship design to achieve its designed efficiency. A model test is the most popular method to estimate hull resistance acting on a ship. Using experimental results, researchers have proposed empirical formulae to estimate the hull resistance for the same series of hull form [1–9]. The hull resistance of a ship has been evaluated in the fundamental calculation. Up to now, empirical formulae have been defined for almost all popular vessels; they have become a powerful designed tool. However, the accuracy of the calculated results given by the empirical formulae is also an important topic that many researchers are interested in [10–15].

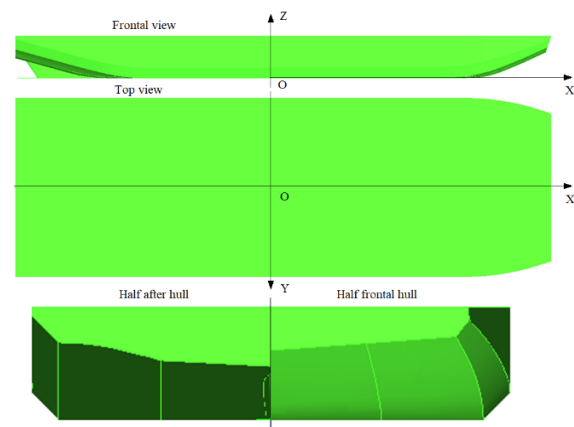
In recent years, Computational Fluid Dynamic (CFD) has gained high popularity for predicting the hull resistance of the ship because of its high efficiency and economy. The accuracy of the CFD results has improved significantly; many studies being done on validating the CFD results showing how to predict the hydrodynamic performances and hull resistance of a ship, and so on [11, 14, 16–22]. Others works have developed new hull forms with various attached devices to improve hydrodynamic performances and to reduce resistance of hull forms by using CFD [11, 12, 14, 19, 22, 23].

Pontoons are being used to support floating bridges across rivers, where water flows are relatively small; in other words: pontoons are working in calm water regions. Nevertheless, from a bridge point of view, estimating a pontoon hull resistance and its hydrodynamic performances are as important as those of a ship. In this study, firstly, resistance acting on a full scale hull of a pontoon in calm water has been investigated by the different valuable empirical formulae such as the Froude, Schoenherr, ITTC1957, and Holtrop formulae. Secondly, the CFD ANSYS-Fluent has been used to compute the hydrodynamic performances and resistance working on the pontoon. The obtained results have been

compared with each other to find how different resistances acting on the hull of the pontoon behave and find out the reasons for those.

**FULL SCALE MODEL OF THE PONTOON**

In this study, a full-scale model of a pontoon is used as a referenced model. Figure 1 shows the body plan of the selected pontoon, and detailed principal dimensions of the pontoon are shown in Table 1.



*Figure 1. Model of the pontoon used for computation*

*Table 1. The main particulars of the pontoon*

Name	Value	Unit
Length over, L	23.40	m
Width, B	8.10	m
Height, H	1.90	m
Design draft, d	0.90	m
Displacement volume, D	138.6	m <sup>3</sup>
Block coefficient, C <sub>B</sub>	0.812	-
Wetted surface area, S <sub>w</sub>	207.2	m <sup>2</sup>
Froude number, F <sub>n</sub>	0.356	-

**EMPIRICAL FORMULAE MOETHED ESTIMATES HULL RESISTANCE**

In the research field of hull resistance, understanding the components of hull resistance and their behavior is essential. That is why researchers have used many methods as

well as using many scaled hull forms. Scaling the obtained resistance results of the experimental model at towing tank to get actual results for the full-scale model, using both empirical formulae and CFD predicted methods [1, 2, 4, 5, 10]. Observation of a ship moving through water indicates two flow features, namely the wave pattern of turbulent flow and wake after the hull of the vessel. Both of these features are affected by hydrodynamic performances and increasing resistance on the ship considerably. The total hull resistance ( $R_T$ ) acting on the ship is defined as the two components: viscous pressure resistance ( $R_p$ ) and viscous friction resistance ( $R_f$ ) acting on the hull of the ship [4–6, 8, 24].

$$R_T = R_p + R_f \quad (1)$$

The total hull resistance coefficient is defined by:

$$C_T = C_p + C_f \quad (2)$$

where:  $C_T$  is the total resistance coefficient;  $C_p$  is the viscous pressure resistance coefficient;  $C_f$  is the viscous friction resistance coefficient.

The resistance coefficients is defined as follows:

$$C_T = \frac{R_T}{0.5\rho V^2 S}; C_p = \frac{R_p}{0.5\rho V^2 S}; C_f = \frac{R_f}{0.5\rho V^2 S} \quad (3)$$

In this study, hull resistance of the ship is investigated by using empirical formulae methods. The first systematic experiments to determine friction resistance in water of thin flat planks were carried out by W. Froude, and R. E. Froude re-examined the results obtained to considerate that the results of planks having surfaces corresponding to those of clean ship hulls or to paraffin wax models could be expressed as the following [2, 3, 5, 24, 25]:

$$R_f = fSV^{1.825} \quad (4)$$

in there:  $f$  depends on length, and gets from R. E. Froude's skin friction  $f$  values;  $S$  is wetted surface area,  $m^2$ ; and  $V$  is velocity,  $m/s$ .

Schoenherr had reported all the available experimental data from plank experiments both in air and water attempting to determine

a formula suitable with the available data. He determined by the following formula [5, 24, 25].

$$C_F = \frac{1}{(3.51\lg_{10} R_e - 5.96)^2} \quad (5)$$

The friction resistance coefficient in accordance with the ITTC1957 formula is defined by [1, 5]:

$$C_F = \frac{0.075}{(\lg_{10} R_e - 2)^2} \quad (6)$$

An approximate power prediction method presented by J. Holtrop and G. G. J. Mennen, the total hull resistance of a ship is defined as follows [4]:

$$R_T = R_F (1 + k_1) + R_{APP} + R_W + R_B + R_{TR} + R_A \quad (7)$$

where:  $R_F$  is viscous frictional resistance according to the ITTC1957 friction formula (6);  $(1 + k_1)$  is form factor describing the viscous resistance of hull form in relation to  $R_F$ ;  $R_{APP}$  is resistance of appendages;  $R_W$  is wave

making and wave breaking resistance;  $R_B$  is additional pressure resistance of bulbous bow near the water surface;  $R_{TR}$  is additional pressure resistance of immersed transom stern;  $R_A$  is model ship correlation resistance.

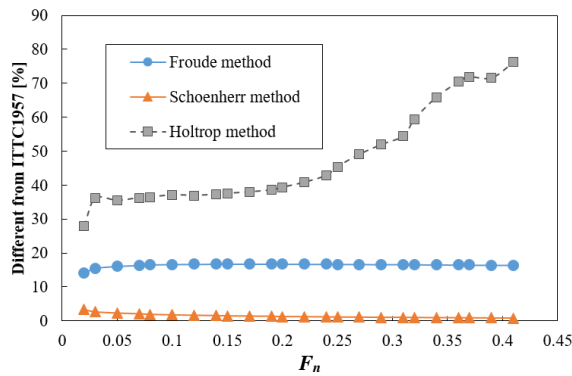


Figure 2. Comparison results of resistance coefficient from the ITTC1957 method

For the pontoon in full scale model as shown in Figure 1, resistance coefficient acting

on the hull of the pontoon in calm water is calculated by the empirical formulae as shown in Table 2.

Table 2 shows the detailed resistance coefficient of the pontoon in the range of the Froude number from 0.02 to 0.41. Figure 2 shows the results of the comparison as per the ITTC1957 method. The results shown that viscous frictional resistance calculated by the Schoenherr formula and ITTC1957 are the same values; however, small differences between them can be seen. The results of viscous frictional resistance calculated by the Froude method are higher than those from ITTC1957 up to 17% in range of Froude number from 0.02 to 0.41, as shown.

Table 2. Calculated results of hull resistance of the pontoon by empirical formula

$F_n$	Resistance coefficient			
	Froude, $C_F$	Schoenherr, $C_F$	ITTC1957, $C_F$	Holtrop, $C_T$
0.020	0.00367	0.00305	0.00315	0.00438
0.030	0.00331	0.00272	0.00280	0.00438
0.050	0.00312	0.00256	0.00262	0.00405
0.070	0.00299	0.00245	0.00250	0.00392
0.080	0.00289	0.00237	0.00241	0.00379
0.100	0.00281	0.00230	0.00235	0.00373
0.120	0.00275	0.00225	0.00229	0.00363
0.140	0.00270	0.00221	0.00225	0.00358
0.150	0.00265	0.00217	0.00221	0.00353
0.170	0.00261	0.00214	0.00217	0.00350
0.190	0.00257	0.00211	0.00214	0.00348
0.200	0.00254	0.00209	0.00211	0.00349
0.220	0.00251	0.00207	0.00209	0.00353
0.240	0.00248	0.00204	0.00207	0.00362
0.250	0.00246	0.00203	0.00205	0.00375
0.270	0.00243	0.00201	0.00203	0.00398
0.290	0.00241	0.00199	0.00201	0.00418
0.310	0.00239	0.00198	0.00200	0.00438
0.320	0.00237	0.00196	0.00198	0.00488
0.340	0.00235	0.00195	0.00197	0.00577
0.360	0.00234	0.00193	0.00195	0.00660
0.370	0.00232	0.00192	0.00194	0.00690
0.390	0.00231	0.00191	0.00193	0.00678
0.410	0.00229	0.00190	0.00192	0.00805

In the range of Froude numbers lower than 0.2, the total resistance coefficient calculated by the Holtrop method are different from other methods by about 38%.

When the Froude number increases higher than 0.2, the different coefficients increase fast and up to 76%, as shown in Figure 2. The different values indicate the number of

other resistance components included in to the Holtrop method.

## INVESTIGATING HULL RESISTANCE OF THE PONTOON BY USING CFD

### Computational fluid domain and mesh

In this section, the hull resistance of the pontoon has been investigated by using commercial CFD code ANSYS-Fluent will be presented. The computation case has been done step by step following the schema for using CFD as well as useful guidelines and many published experiences in using CFD to

solve hydrodynamic ship problems reported by the International Towing Tank Conference (ITTC) [5, 10, 12, 19, 21–23]. The computational fluid domain has been designed in the limited dimension of 6 L × 1.5 L × 1.5 L instead of 140 m length, 35 m calculating the width, and 35 m height. Meshing the computed domain in the structured *H*-grid is of 2.83 million grids. The turbulent viscous model *k- $\omega$*  is applied to unsteady flow, and the Volume of Fluid (VOF) multiphase model has been used. The inlet and outlet of the computed domain have been set up with a velocity inlet and pressure outlet. Figure 3 shows the mesh of the computational fluid domain.

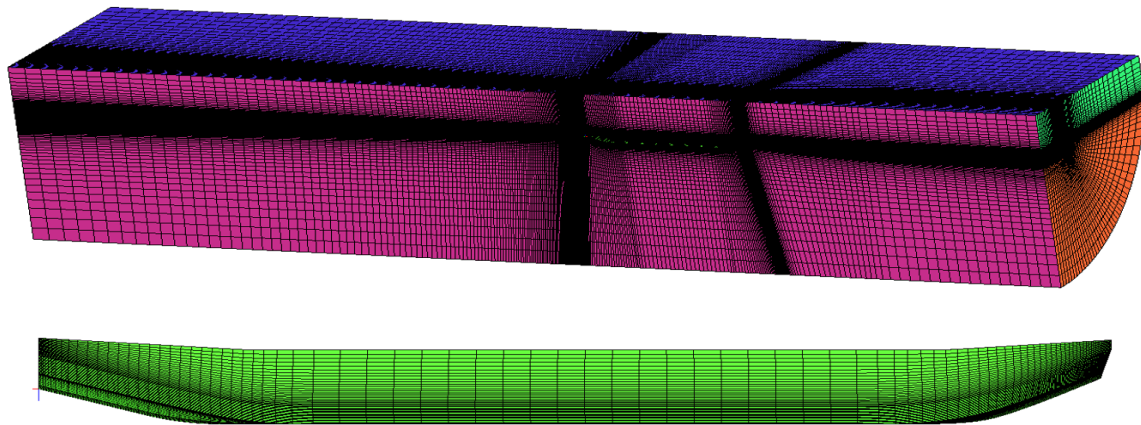


Figure 3. Mesh of the computational fluid domain

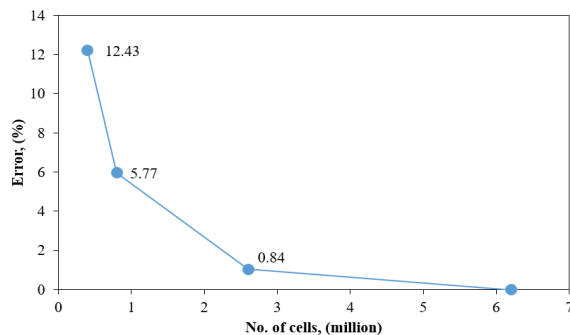


Figure 4. Effect of mesh on CFD results of total resistance coefficient of the pontoon

The effects of a mesh of the computed domain on the CFD results have been reported in many previous papers [7, 11, 12, 14, 16, 18–23]. This study uses several different meshes of

the computed domain to simulate the pontoon in calm water at the Froude number of 0.36. Table 3 shows a detailed mesh of the computed domain and the computed hull resistance coefficients of the pontoon in the different calculated cases. Figure 4 shows the curves of the mesh effect on the computed hull resistance coefficient of the pontoon in calm water at the Froude number of 0.36.

Figure 4 shows the results of the different hull resistance coefficients in the different computed cases, as shown in the Table 3. The error between the calculated results was less than 12.43% when the value of  $Y^+$  was less than 8.325, and the resistance coefficient was the same for all computed cases when the mesh number was over 2.626 million instead of a  $Y^+$  value below 0.897, as shown.

Table 3. Mesh of computed domain and the CFD results of hull resistance

$Y^+$	Total elements ( $\times 10^6$ )	Minimum face area, ( $\times 10^{-8} \text{ m}^2$ )	Maximum face area, ( $\times 10^{-4} \text{ m}^2$ )	Minimum volume, ( $\times 10^{-6} \text{ m}^3$ )	Maximum volume, ( $\times 10^{-2} \text{ m}^3$ )	$C_T$ ( $\times 10^{-2}$ )
8.3251	0.4235	1.9521	12.2825	5.0682	7.2656	0.01112
5.8823	0.8366	1.6223	9.26285	2.6352	2.9372	0.00932
0.8972	2.6269	0.0519	2.01281	0.3267	1.8098	0.00981
0.2436	6.2321	0.0162	1.89285	0.0563	1.5219	0.00991

**CFD results of hull resistance acting on the pontoon**

In this section, the hydrodynamic performance and hull resistance of the pontoon

investigated by using the CFD is presented. Figures 5–6 show pressure distribution around the hull of the pontoon at the center plane of the computed domain and over the hull surface of the pontoon in different Froude numbers.

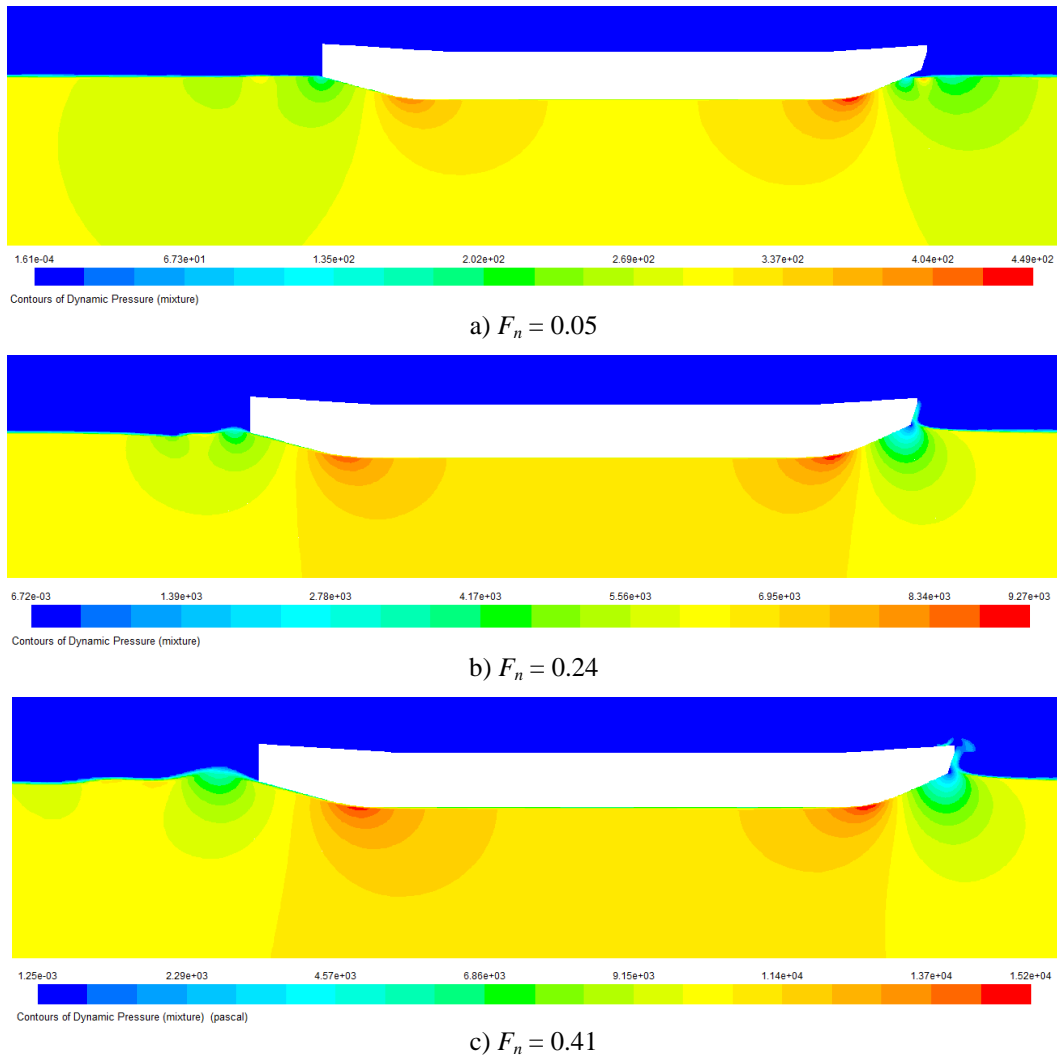


Figure 5. Dynamic pressure distribution around the hull of the pontoon at the center plane of the computed domain

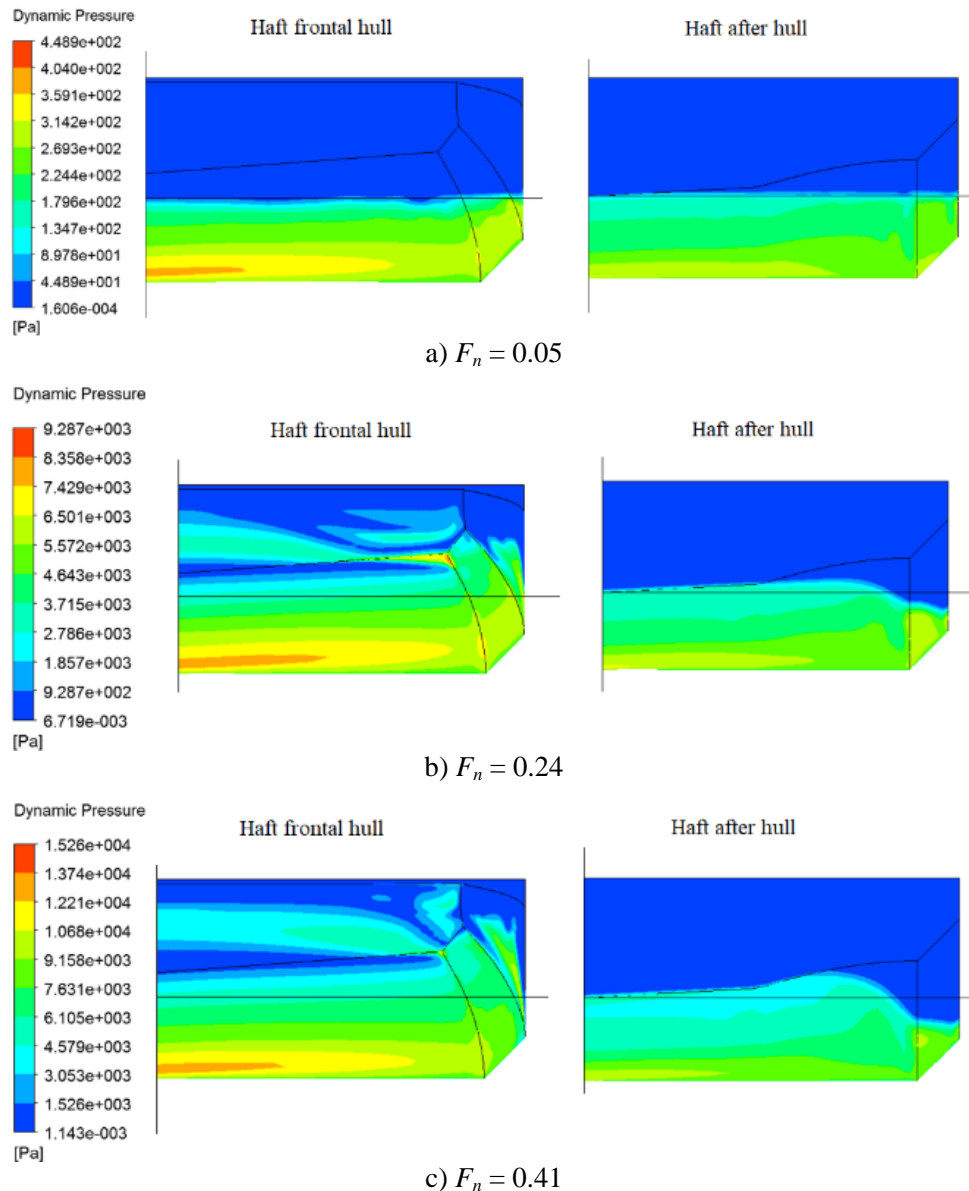


Figure 6. Dynamic pressure distribution over the hull surface of the pontoon

The results, as shown in Figures 5–6, clearly show the effect of the Froude number on dynamic pressure distribution around the pontoon and over the hull surface of the pontoon. In the results, the red and yellow regions indicate that the dynamic pressure around and over the hull surface is high, and the blue area indicates a lower dynamic pressure region over the surface of the pontoon's hull. In high Froude number, the bow waves are high and increase a larger

dynamic pressure region over the bow surface of the pontoon. Figure 7 shows the results of the resistance coefficient of the pontoon investigated by the different methods. The detailed results are shown in Table 3, and the CFD results of the hull resistance coefficient of the pontoon are shown in Table 4.

In the results shown, the viscous frictional resistance coefficient acting on the pontoon computed by the CFD is in good agreement with those of the Froude, Schoenherr, and

ITTC1957 methods. The total resistance coefficient calculated by the CFD compared with the Holtrop way is higher than 25% in the range of Froude number lower than 0.24

and increasing fast up to 50% at the high Froude number. The results agree with those of the pressure distribution around the pontoon, as shown.

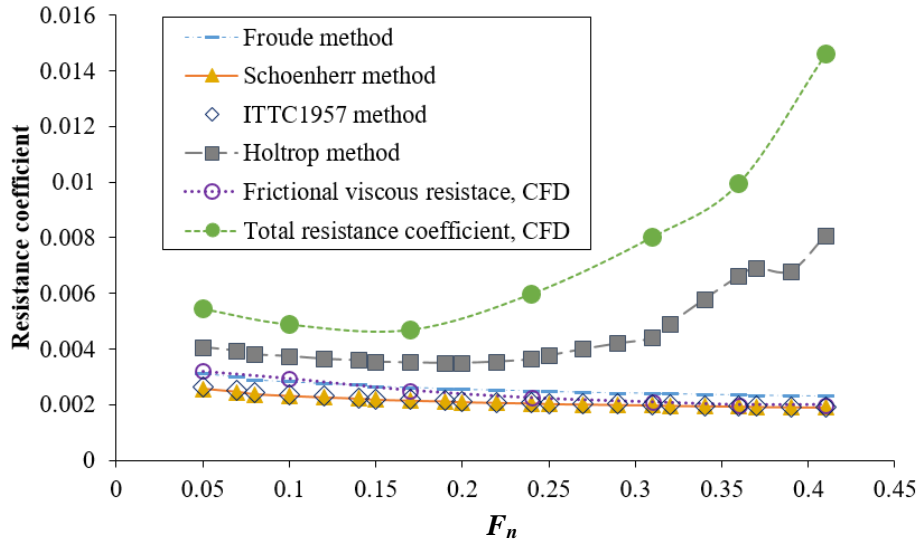


Figure 7. Investigated hull resistance coefficient of the pontoon

Table 4. Resistance acting on the pontoon investigated by the CFD

$F_n$	Resistance, (N)			Resistance coefficient		
	$R_f$	$R_p$	$R_T$	$C_f$	$C_p$	$C_T$
0.05	198.090	138.236	336.326	0.00320	0.00223	0.00543
0.10	736.021	476.103	1,212.124	0.00298	0.00193	0.00491
0.17	1,731.001	1,480.324	3,211.325	0.00253	0.00216	0.00469
0.24	3,001.981	5,008.131	8,010.112	0.00223	0.00373	0.00596
0.31	4,630.088	13,175.127	17,805.215	0.00208	0.00593	0.00802
0.36	6,007.112	24,089.003	30,096.115	0.00199	0.00797	0.00996
0.41	7,856.321	49,754.910	57,611.231	0.00199	0.01260	0.01459
0.44	9,856.025	61,679.088	71,535.113	0.00213	0.01331	0.01544

## CONCLUSION

This study investigated the hull resistance of the full-scale pontoon in calm water using the different empirical formulae methods such as the Froude, Schoenherr, ITTC1957, and Holtrop methods and using the CFD simulation. The obtained results show the restrictions of the empirical formulae applied to calculate the hull resistance of the ship have been found. The empirical formulae have given close results of viscous frictional resistance acting on the hull of the pontoon in comparison between the different methods. However, the

viscous pressure resistance component calculated by the empirical formula is much less than the CFD results at a lower Froude number of 0.24. The error is up to 25% and increases fast up to 50% at Froude number of 0.44. The results suggest that a pontoon's body plane is the only concerned variable at a low Froude number.

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