JUDD OFELT ANALYSIS AND OPTICAL PROPERTIES OF Eu$^{3+}$ DOPED TELLURITE GLASSES

TRAN THI HONG
Da Nang University of Education

PHAN TIEN DUNG
Institute of Materials Science, Vietnam Academy of Science and Technology

VU XUAN QUANG
Duy Tan University

E-mail: dungpt63@gmail.com

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Abstract. In this work, the structural characteristic and photoluminescence properties of Eu$^{3+}$ doped $B_2O_3$-$TeO_2$-$ZnO-Na_2O$ glasses were investigated. These glasses were prepared by a melting method in air, combined with thermal annealing at 350 °C, 450 °C and 550 °C for different duration times. The structural analysis results of these glasses revealed the formation of micro-crystals in the annealed host glass. The photoluminescence spectra of Eu$^{3+}$ doped in these samples were observed. The local vibration mode around Eu$^{3+}$ ions was investigated by the phonon side-band (PSB) associated with $^7F_0$$\rightarrow$$^5D_2$ transition of Eu$^{3+}$. Judd-Ofelt parameters were then evaluated based on photoluminescence spectra and the luminescence intensity ratios of $^5D_0$$\rightarrow$$^7F_J$ ($J = 2, 4$ and $6$) to $^5D_0$$\rightarrow$$^7F_1$ transition were predicted. The obtained results were then used to calculate $\Omega_2$, $\Omega_4$, $\Omega_6$ parameters based on Judd-Ofelt theory. These $\Omega_2$, $\Omega_4$, $\Omega_6$ parameters allow to derive radiative properties of Eu$^{3+}$ ions in glass material such as transition probabilities, radiative lifetimes and peak stimulated emission cross-section for the $^5D_0$$\rightarrow$$^7F_J$ transitions.

Keywords: Optical properties, luminescence, Judd-Ofelt theory, rare earth, Tellurite glasses.

I. INTRODUCTION

Oxide glasses are the most stable host matrices for practical applications due to their high chemical durability and thermal stability. Among the oxide glasses, tellurite glasses have proved to be interesting host for lanthanide ions, both from a fundamental and applied point of view. It is well known that the non-radiative loss is dominated by the highest energy phonon available in the matrix. Therefore, it is meaningful to select a host material that its maximum phonon energy is as low as possible. In silica, this phonon energy is reasonably large (about 1100 cm$^{-1}$). However, it is quite low for chalcogenide glasses (about 300 cm$^{-1}$), which lack many desirable features of silica-based glasses including mechanical strength and chemical durability. Tellurite glasses represent a compromise one among the desire for low phonon energy (650-750 cm$^{-1}$) [1–3] host...
couple with the need to retain mechanical strength and process temperatures... However, less spectroscopic study on Borate-tellurite-zinc-sodium based glass was reported.

Among the Ln\(^{3+}\) ions used to optically activate the glass matrices, the trivalent europium ion Eu\(^{3+}\) is the mostly choice due to the fact that Eu\(^{3+}\) \((4f^6)\) ions emit narrow band, almost monochromatic light, long lifetimes of optical active states. Eu\(^{3+}\) is also has been studied widely because of its simple electronic energy level scheme. Eu\(^{3+}\) ions exhibit pure magnetic and electric dipole transitions which are very sensitive probe for the rare earth ion site structure symmetry. The transition probability of hypersensitive transition \((^5D_o \rightarrow ^7F_2)\) of Eu\(^{3+}\) ion is depressed under higher symmetric environment whereas the magnetic dipole transitions are not affected by the environment. Their emission intensities are often used as internal standard [4, 5].

**II. EXPERIMENTS**

Using melting method, the 40B\(_2\)O\(_3\).40TeO\(_2\).10ZnO.10Na\(_2\)O glass containing Eu\(_2\)O\(_3\) 1 mol% concentration was prepared by two processes: melting followed by heated-treatment. B\(_2\)O\(_3\), TeO\(_2\), ZnO, Na\(_2\)CO\(_3\) and Eu\(_2\)O\(_3\) were used as starting materials. All components above were mixed by grinding them in a mortar gate carefully and dried at 100 °C in the oven for 3h. The mixture was then melted at 1200 °C in a Pt crucible in air for 2h. The fining step was carried out by keeping the melt at the temperature of 1150 °C for 15min. After slowly cooling the melt down to room temperature, the transparent and colorless glass was obtained. Finally, obtained glass was annealed in oven at 350 °C for 10h, 450 °C for 15h and 550 °C for 24h, respectively. Then was cut and polished for all optical measurements.

X-ray diffraction measurement was done on a XRD-D5000 SIEMENS diffractometer. Excitation and emission spectra of the samples were measured on a Horiba FluoroLog Spectrophotometer FL3-22 using a 450W xenon lamp source, monochromator (f/3.6 Czeny-Turner, double grating, all reflective optics) and R928P photomultiplier. Signals were recorded under computer control software FluorEssence 2.0 (powered by Origin 7.5). All the measurements were done at room temperature.

**III. RESULTS AND DISCUSSION**

**III.1. Structural characterization**

Generally, melting is a very strong method to fabricate glasses. Beside, heated-treatment for as-prepared glasses is also an important process because it makes structure of the glasses to be more stable. During this process, micro-crystals can be formed in the host glass which is called glass-ceramic materials.

XRD patterns of the glass samples are presented in Fig. 1. This figure shows the XRD patterns of the glass samples annealed at 350 °C for 10h (a), 450 °C for 15h (b) and 550 °C for 24h (c). The results of the structural analysis indicate that the glass sample annealed at 350 °C for 10h exhibits a pure amorphous phase, while the samples annealed at...
450 °C for 15 h and 550 °C for 24 h exhibit a mixture of amorphous and crystalline phases. It is known that the glass crystallization process is strongly dependent on the conditions of thermal annealing such as temperature, duration time and host components. Therefore, these preliminary results suggest the technological process preparing the glass-ceramic materials [6, 7].

III.2. Optical properties

a. Excitation photoluminescence (PLE)

The excitation photoluminescence spectra for 612nm red emission of 1 mol% Eu³⁺ doped samples are shown in Fig. 2. The transitions of PLE were assigned (originating from ⁷F₀ and ⁷F₁) based on free-ion energy level structure and by taking into account both the electric and magnetic dipole contributions. There are fifteen obvious excitation peaks parking at 299nm, 304nm, 319nm, 327nm, 361nm, 365nm, 377nm, 382nm, 394nm, 400nm, 414nm, 465nm, 472nm, 526nm, 533nm. Among them, the intensity of 394nm excitation peak is greatest.

The PSB of the ⁵D₂−⁷F₀ transition of the Eu³⁺ ion was observed in the excitation spectra shown in Fig.2. The PSB of the B₂O₃-base glass is attributed to the stretching vibration modes of B-O⁻ and B-O of B₂O₃ and BO₄ units in tetra- and di-borate groups [8], where −O⁻ and −O stand for the non-bridging oxygen (NBO) and bridging oxygen (BO), respectively. In fact, PSB is influenced both by the stretching vibration mode of NBO in the neighborhood of the Eu³⁺ ions and by the stretching vibration modes of NBO and BO which are apart from the Eu³⁺ ions.

The energy level diagram (Fig. 3) of Eu³⁺ shows the energy gaps among the levels of ⁵G₂, ⁵L₆, ⁵D₃, ⁵D₂, ⁵D₁ and ⁵D₀. The emission efficiencies of ⁵D₃, ⁵D₂ and ⁵D₁ levels are related to the non-radiative rate Wₜ. Wₜ can be expressed by:

\[ W_{NR} = W_P + W_{ET} \] (1)

where \( W_P \) is the multiphonon decay rate and \( W_{ET} \) is the relaxation rate by energy transfer. For the lower concentration of Eu³⁺ doping, the contribution of \( W_{ET} \) can be ignored temporarily, and the factor dominating the quantum efficiency is \( W_P \), which is associated with the phonon energy, \( W_P \).
is expressed by:

\[ W_p = W_0 \exp \left( \frac{-\alpha \Delta E}{\hbar \omega} \right) \]  (2)

where \( \Delta E \) is the optical energy gap to the next lower level and \( \hbar \omega \) is the phonon energy of the glass and \( W_0 \) is the transition probability extrapolated to zero energy gap which is independent to the electronic nature of the RE ion. \( \alpha = \ln \left[ \frac{\Delta E}{(\hbar \omega g)} \right] \), where, \( g \) is the electron-phonon coupling strength [9]. According to Eq. (2), \( W_{NR} \) in silicate and phosphate should be much larger, with higher maximum-phonon energies \( (\hbar \omega \sim \text{1100 cm}^{-1} \text{ and } \sim \text{1300 cm}^{-1}, \text{respectively}) \) than that in tellurite glass \( (\hbar \omega \sim \text{750 cm}^{-1}) \). It is the main reason why the emissions of Eu\(^{3+} \) ions from \( ^5D_3, ^5D_2 \) and \( ^5D_1 \) levels could not be observed in silicate and phosphate glasses but can be recorded in tellurite \((40\text{B}_2\text{O}_3.40\text{TeO}_2.10\text{ZnO}.10\text{Na}_2\text{O}.1\text{Eu}^{3+})\) glasses clearly.

b. Photoluminescence (PL)

Fig. 4 shows the photoluminescence spectra of 1 mol% Eu\(^{3+} \) doped samples. These spectra were obtained by exciting the \( ^5L_6 \) state using the 394 nm wavelength of a broad band xenon lamp source. Emissions are mainly observed for \( ^5D_0 \rightarrow ^7F_J (J=0, 1, 2, 3, 4) \) transitions (with maximums at 578 nm; 591 nm; 612 nm; 653 nm and 700 nm, respectively) and a few weak emissions are noticed for \( ^5D_1 \rightarrow ^7F_0,1,2 \) (with the maximums at 527 nm; 534 nm; 553 nm, respectively) which are assigned in Fig. 4. It can be seen obviously that increasing the temperature of the heated-treatment process leads to the intensity increase of the spectrum significantly.

The emission intensities of \( ^5D_0 \rightarrow ^7F_{2,4} \) transitions are induced electric dipole allowed and depend strongly on the local symmetry around Eu\(^{3+} \) ions. Moreover, the \( ^5D_0 \rightarrow ^7F_2 \) is said to be hypersensitive transition (under the selection rule \( \Delta J =2 \)) to the surrounding environment, whereas the transition \( ^5D_0 \rightarrow ^7F_1 \) is magnetic dipole allowed and independent of the local symmetry.

Therefore, the ratio of integrated emission intensity of the \( ^5D_0 \rightarrow ^7F_2 \) transition to that of the \( ^5D_0 \rightarrow ^7F_1 \) transition, defined as fluorescence intensity ratio \( R \), is the spectroscopic key to estimate the deviation from the site symmetry of the Eu\(^{3+} \) ions. Sometime, \( R \) is also defined as asymmetry ratio. In our experiments, the emission spectra were recorded for the sample \( 40\text{B}_2\text{O}_3.40\text{TeO}_2.10\text{ZnO}.10\text{Na}_2\text{O}.1\text{Eu}_2\text{O}_3 \) excited by the wavelength of 394nm. The fluorescence intensity ratio \( R \) were found to be 4.1; 3.9 and 3.8 corresponding to the glass samples heated-treatment at 350 °C-10 h; 450 °C-15h and 550 °C-24 h, respectively. According to Kumar \textit{et al.} [10], most of the Eu\(^{3+} \) doped glasses exhibit the \( R \) values in the range of 3.5-4.2. This indicates the potential of Borate-tellurite-zinc-sodium: Eu\(^{3+} \) glass as a promising laser and red luminescence material.
III.3. Judd-Ofelt analysis

The Judd-Ofelt theory was often used to calculate the intensity parameters $\Omega_\lambda$ ($\lambda=2, 4, 6$). The intensity parameters $\Omega_\lambda$ could be obtained from absorption spectra. But sometimes, it is very difficult to measure absorption spectra. However, the strong luminescence is a characteristic feature of many europium doped materials [11]. Therefore, the Judd-Ofelt (J-O) analysis by emission spectra is frequently used for the Eu$^{3+}$ doped host matrices.

The emission spectra of Borate-tellurite-zinc-sodium: Eu$^{3+}$ ion excited by 394 nm light are shown in Fig.4. Among them, three main emission peaks $^5D_0 \to ^7F_1$, $^5D_0 \to ^7F_2$ and $^5D_0 \to ^7F_4$ were used to calculate the J-O parameters.

The $^5D_0 \to ^7F_1$ is the magnetic dipole transition and its spontaneous emission probability $A_{md}$ is given by the following expression [4, 5]:

$$A_{md} = \frac{64\pi^4}{3h} \frac{v^3}{2J+1} n^3 S_{md}$$

where $v$ is the wavenumber of transition, $h$ is the Planck constant, $J$ is the total angle momentum of the excited state, $n$ is the refractive index and $S_{md}$ is the magnetic-dipole line strength which is a constant and independent of the host material.

The $A_{md}$ can be estimated by using the reference value of $A'_{md}$ published somewhere and the relationship $A_{md} = (n/n')^3 A'_{md}$, where $A'_{md}$ and $n'$ are the spontaneous emission probability and refractive index of the reference material, respectively. For example, in the case of lithium fluoroborate glasses doped with 1 mol % Eu$^{3+}$, $A'_{md} = 51.9$ s$^{-1}$ and $n' = 1.539$ [12].

The $^5D_0 \to ^7F_{J=2,4,6}$ transitions are electronic dipole allowed. The spontaneous emission probability $A_{ed}$ of electronic transition is given by:

$$A_{ed} = \frac{64\pi^4 e}{3h} \frac{v_J^3}{2J+1} \frac{n(n^2 + 2)^2}{9} S_{ed}$$

where $v_J$ is the wavenumber of transition $^5D_0 \to ^7F_J$; $e$ is the electron charge; $h$ is the Planck constant; $n$ is the refractive index; $J$ is the total angle momentum of excited state and $S_{ed}$ is the electric-dipole line strength of the transition [13].

The emission intensity $I$ of a given transition is proportional to the area $S$ under the emission curve: $I = h\nu A_r N \alpha S$. Where $h\nu$ is the transition energy, $A_r$ is the radioactive transition rate and $N$ is the population of emitting level ($^5D_0$). Thus, $\Omega_\lambda$ parameters could be evaluated simply by the ratio of the intensity of the $^5D_0 \to ^7F_{J=2,4,6}$ transitions to the intensity of $^5D_0 \to ^7F_1$ transition:

$$\frac{\int I d\nu}{\int I d\nu} = \frac{A_J}{A_1} = \frac{e^2}{S_{md}} \frac{v_J^3}{v_1^3} \frac{n(n^2 + 2)^2}{9n^3} \Omega_J \|U^J\|^2$$

where $\|U^J\|^2 \equiv \langle \Psi J | U^J | \Psi J' \rangle^2$ is the square of the matrix elements of the tensor operator, which connects $|\Psi J\rangle$ to final state $|\Psi J'\rangle$ and is considered to be independent of host matrix. The value of $\|U^J\|^2$ for every transition of the RE$^{3+}$ ions could be found in the published tables [12, 13]. As seen from Eq. (5), $\Omega_2$ and $\Omega_4$ can be evaluated independently from the emission transitions of $^5D_0 \to ^7F_2$ and $^5D_0 \to ^7F_4$. But, $\Omega_6$ cannot be evaluated because of limitation of our experimental conditions. Since the emission transition $^5D_0 \to ^7F_6$ at about 810nm has not been observed from the emission spectra, $\Omega_6$ parameter could not be determined in our experiment because the $^5D_0 \to ^7F_6$ emission
intensity is usually very weak compared to intensities of the $^5D_0 \rightarrow ^7F_2$ and $^5D_0 \rightarrow ^7F_4$ transitions. The calculated $\Omega_2$ and $\Omega_4$ parameters are presented in Table 1.

### Table 1. Judd-Ofelt parameters ($\Omega_\lambda \times 10^{-20}$ cm$^2$)

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<thead>
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<th>$\Omega_\lambda$</th>
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<tr>
<td></td>
<td>(350 °C-10 h)</td>
<td>(450 °C-15 h)</td>
<td>(550 °C-24 h)</td>
</tr>
<tr>
<td>$\Omega_2$</td>
<td>4.872</td>
<td>4.718</td>
<td>4.614</td>
</tr>
<tr>
<td>$\Omega_4$</td>
<td>1.463</td>
<td>1.487</td>
<td>1.519</td>
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<tr>
<td>$\Omega_6$</td>
<td>—</td>
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From Table 1, the $\Omega_2$ value is greater than $\Omega_4$ and the value of $\Omega_6$ cannot be evaluated in every samples. Thus, it can be concluded that the radiative transition probabilities are mainly dependent on the $^5D_0 \rightarrow ^7F_2$ red hypersensitive emission transition. This result is in agreement with that of the other tellurite glasses [14].

According to Ref. [15, 16], the fluorescence intensity ratio $R$ of $^5D_0 \rightarrow ^7F_2$ to $^5D_0 \rightarrow ^7F_1$ transition was used to establish the degree of asymmetry in the vicinity of Eu$^{3+}$ ions and Eu-O covalent. Moreover, the $R$ value also depends on the J-O parameter $\Omega_2$, which was used to explain the short-range effects. Therefore, change of $R$, and in turn, $\Omega_2$ give information about the short range effect on local structure around Eu$^{3+}$ ions and Eu-O covalent. The higher value of $R$, the lower symmetry around the Eu$^{3+}$ ions and the higher the Eu-O covalent.

The Judd-Ofelt theory parameters not only can give the information on local structure and binding state of RE ions in host matrices, but also from the parameters $\Omega_\lambda$, several important optical properties such as branching ratio, relative transition probabilities, lifetimes of the excited states... could be evaluated. The radiative transition probability for transition $\psi J \rightarrow \psi'J'$ is given by:

$$A(\psi J \rightarrow \psi'J') = A_{ed} + A_{md}$$

The calculated radiative life time $\tau_{cal}$ of the excited state can be obtained from $A_{total}$:

$$A_{total}(\psi J) = \sum_{\psi'J'} A(\psi J, \psi'J') = 1/\tau_{cal}.$$ 

So in order to receive $\tau_{cal}$ of $^5D_0$ state, it is necessary to evaluate the radiative transition probabilities of the $^5D_0 \rightarrow ^7F_1$, $^5D_0 \rightarrow ^7F_2$ and $^5D_0 \rightarrow ^7F_4$ transitions. Because the reduced matrix is small, the $^5D_0 \rightarrow ^7F_6$ transition is also negligible, so the $A_{ed}$ of this transition can be negligible in $\tau_{cal}$. The branching ratio is given by $\beta_R(\psi J, \psi'J') = A(\psi J, \psi'J')/A_{total}(\psi J)$.

### Table 2. The branching ratio $\beta_R(^5D_0 \rightarrow ^7F_2)(\%)$, the life time of the excited $\tau_{cal}$ and $\tau_{exp}$ of samples.

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<th>The sample</th>
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<tbody>
<tr>
<td></td>
<td>(350 °C-10 h)</td>
<td>(450 °C-15 h)</td>
<td>(550 °C-24 h)</td>
</tr>
<tr>
<td>$\tau_{cal}(ms)$</td>
<td>2.984</td>
<td>3.118</td>
<td>3.269</td>
</tr>
<tr>
<td>$\tau_{exp}(ms)$</td>
<td>1.181</td>
<td>1.235</td>
<td>1.244</td>
</tr>
<tr>
<td>$\beta_R(^5D_0 \rightarrow ^7F_2)(%)$</td>
<td>72.56</td>
<td>73.32</td>
<td>75.14</td>
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From Table 2, the calculated lifetime $\tau_{\text{cal}}$ of the excited state ($^5D_0$) of this Borate-tellurite-zinc-sodium is longer than the experimental lifetime $\tau_{\text{exp}}$. This is perfectly reasonable. The experimental lifetime ($\tau_{\text{exp}}$) is always contributed from both of conversions: emission and non-emission. Meanwhile, the life time ($\tau_{\text{cal}}$) is only contributed from emission.

**IV. CONCLUSION**

1 mol% Eu$^{3+}$-doped 40B$_2$O$_3$.40TeO$_2$.10ZnO.10Na$_2$O glasses were studied. In the case of samples heated at 450 °C for 15 h and 550 °C for 24 h, the crystalline formation is dominated. These results revealed that 450 °C and 15 h are the temperature and duration time, needed to form crystalline phases in the Borate-tellurite-zinc-sodium glass. The PSB of the $^5D_2 \rightarrow ^7F_0$ transition of Eu$^{3+}$ ions was evaluated from the excitation spectrum. Emission spectra were then used to calculate $\Omega_2$, $\Omega_4$ parameters based on Judd-Ofelt theory. Obtained results of the $\Omega_2$, $\Omega_4$ parameters revealed that the radiative transition probabilities depend mainly on the $^5D_0 \rightarrow ^7F_2$ red hypersensitive emission transition. A relatively higher $\Omega_2$ value of the sample heated at 350 °C for 10 h compared to the samples heated at 450 °C for 15 h and 550 °C for 24 h could be due to the higher asymmetry around Eu$^{3+}$ ions in this non-linear optical material. The high brightness and short lifetime of $^5D_0 \rightarrow ^7F_2$ emission show the good potential application of Borate-tellurite-zinc-sodium glass in photonics.

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